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# The Accu-stat

Section 13335, Group 4

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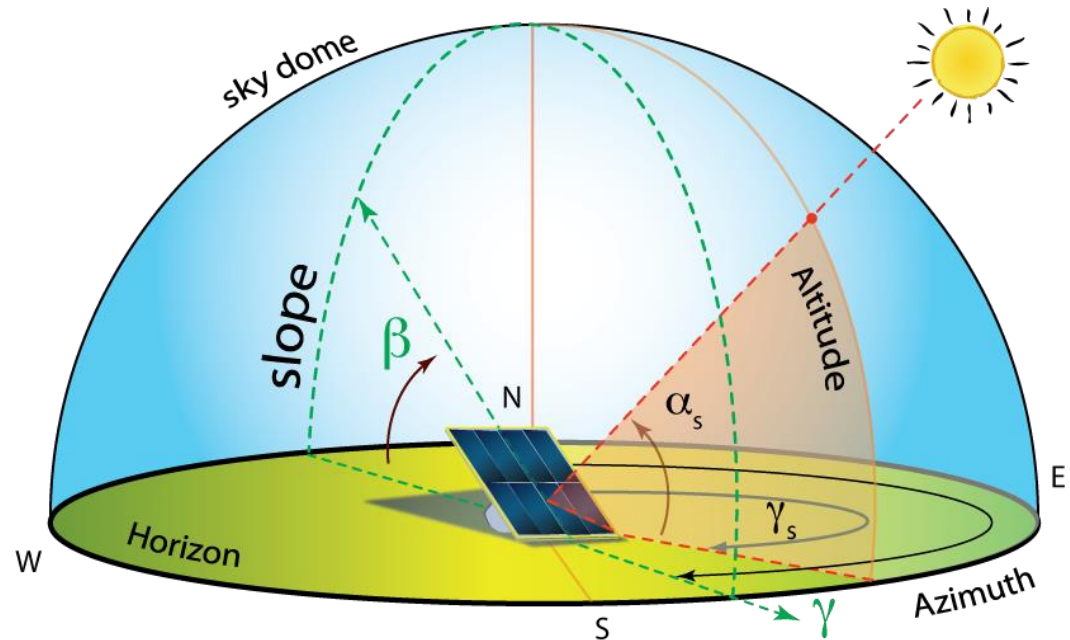
# Presentation Outline



# Value Proposition

## Accuracy

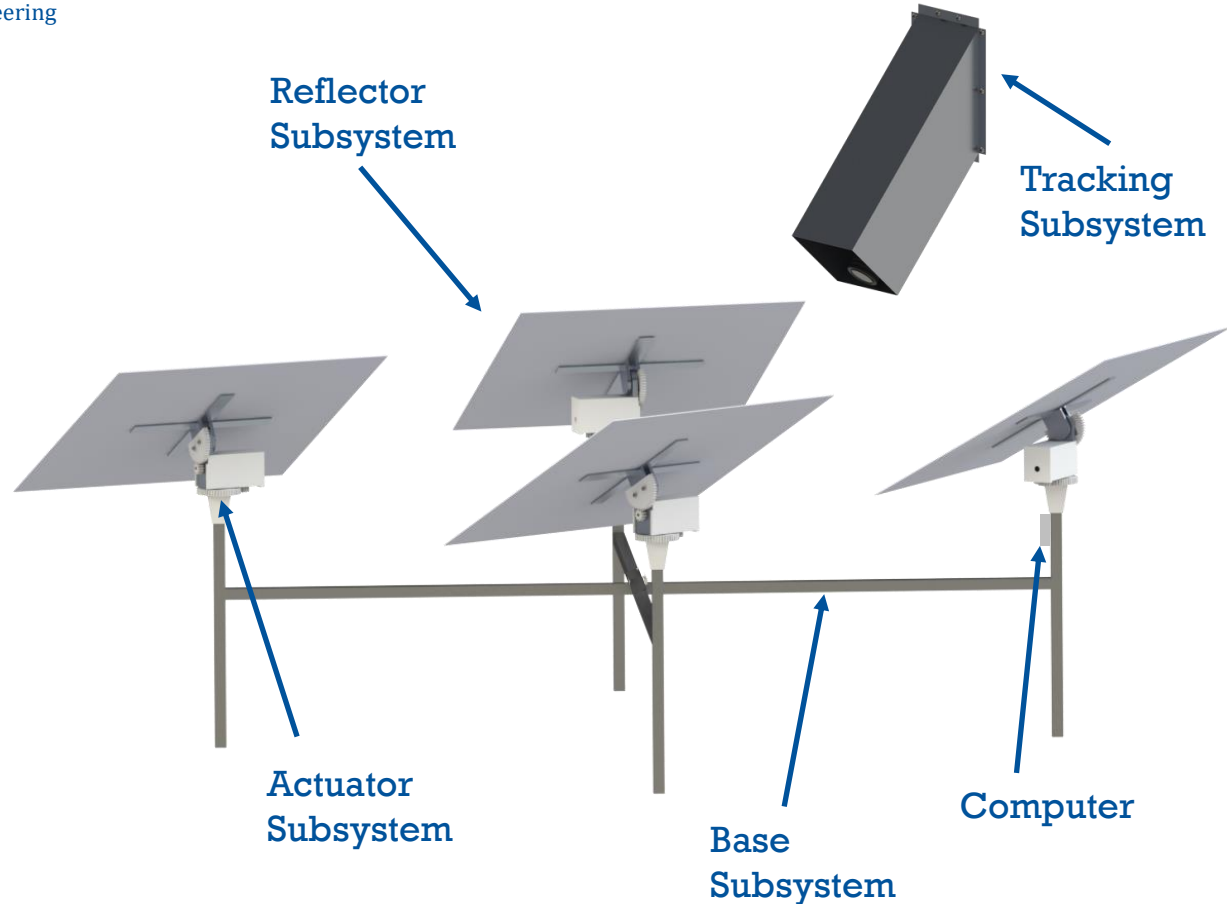
- Actuation
- Tracking



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# Product Overview

- Full assembly is broken down into four subsystems:
  - Base
  - Actuator
  - Reflector
  - Tracking
- Size: 2.1 m x 2.1 m x 0.78 m (max)
- 1 central computer per module
- 2 motor system per heliostat
- Attachable camera mount to central tower

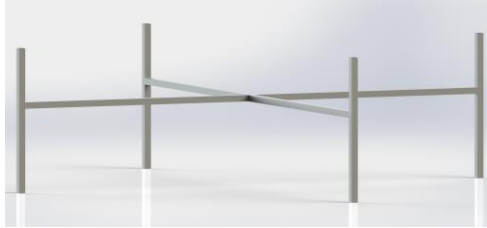


## Basic Functionality

### High Accuracy Tracking at a Low Cost



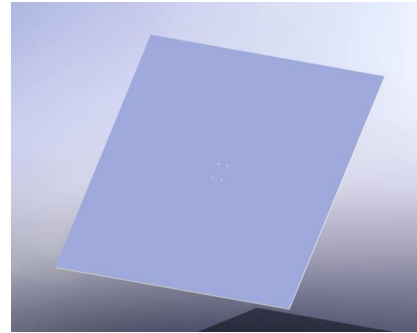
# Subsystem Breakdown



Base



Actuator



Reflector

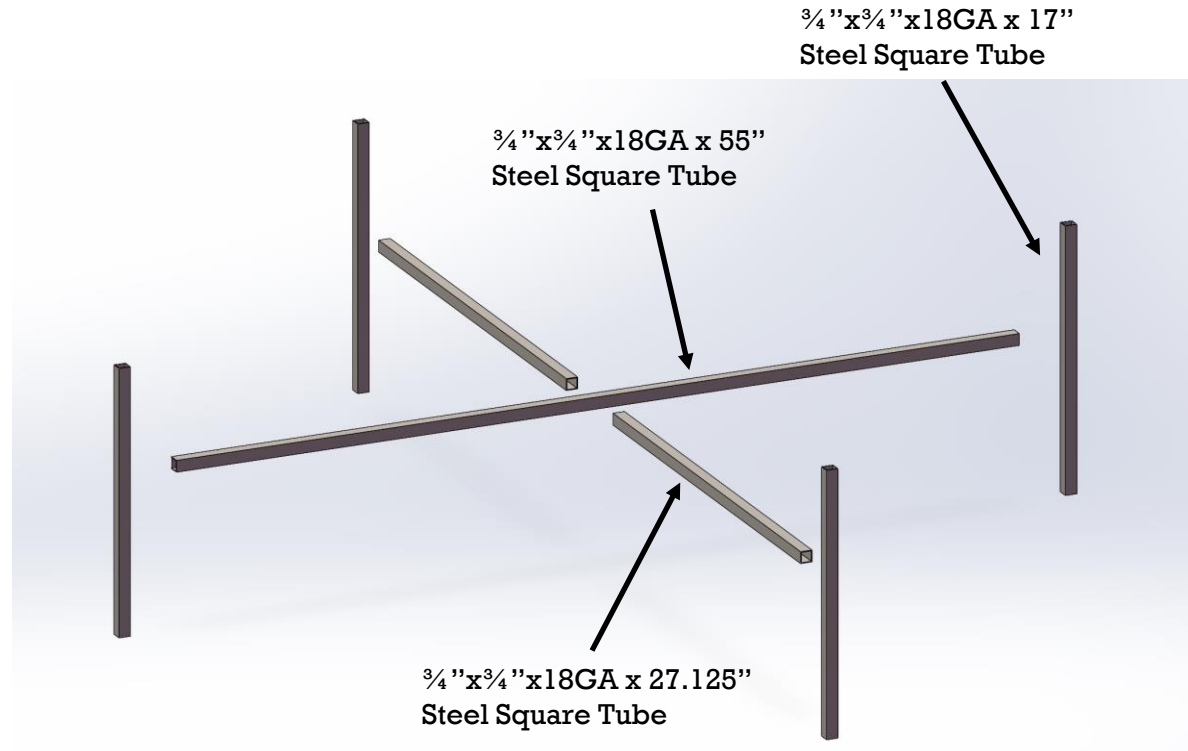


Tracking

# Base Subsystem

## Key Features

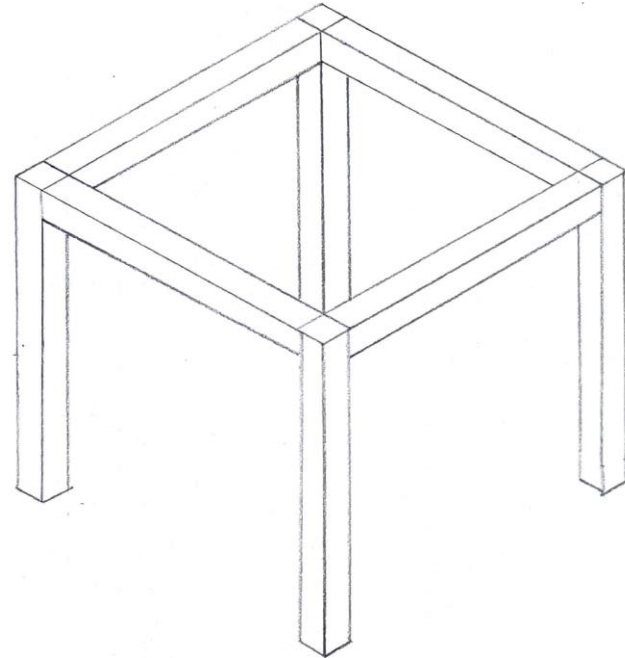
- Minimal Shading
- Will survive in highest winds
- Easy Assembly
- Minimizes Material



# Base Subsystem

## Original Concept

- Cross beams offer extra support
- Eliminates concrete foundation
- Low cost
- Easy manufacturing

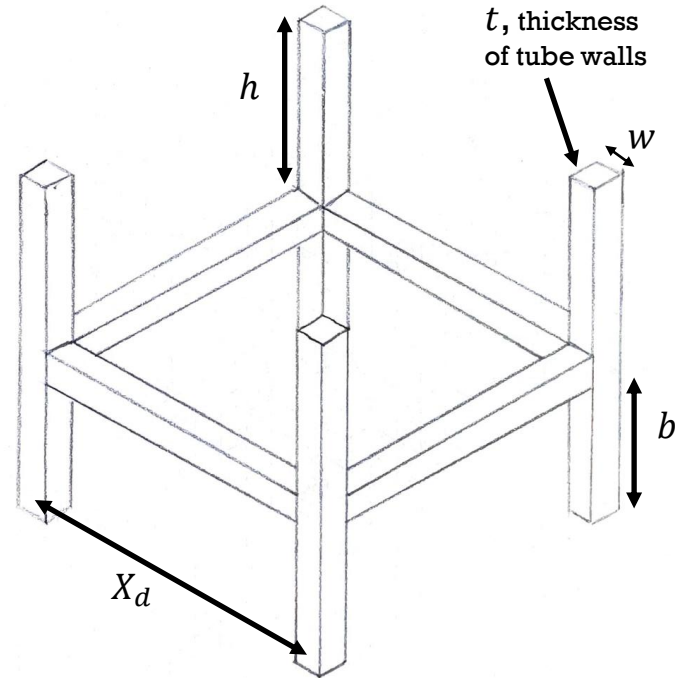




# Base Subsystem

## Revised Starting Concept

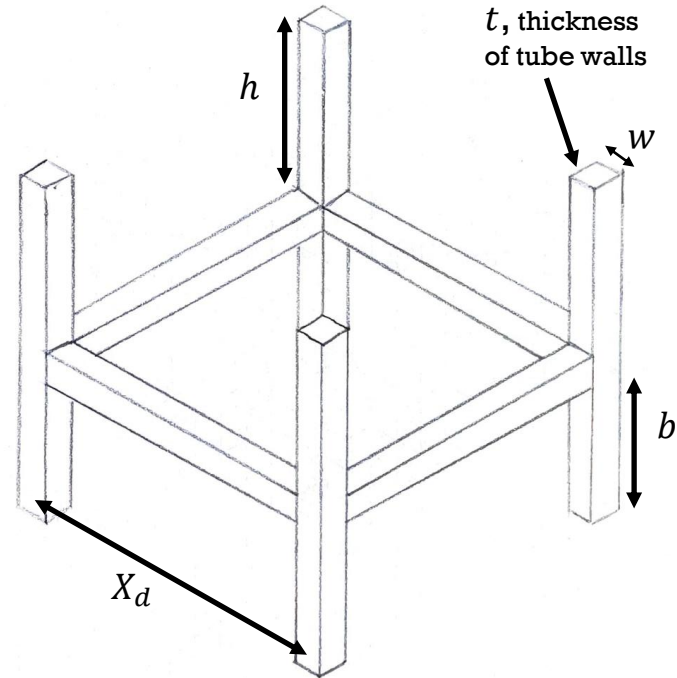
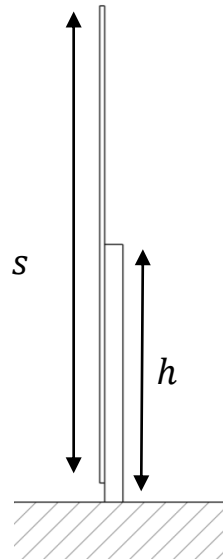
- Section  $b$  buried in ground
- Determine variables and material



# Base Subsystem

## Revised Starting Concept

- Section  $b$  buried in ground
- Determine variables and material

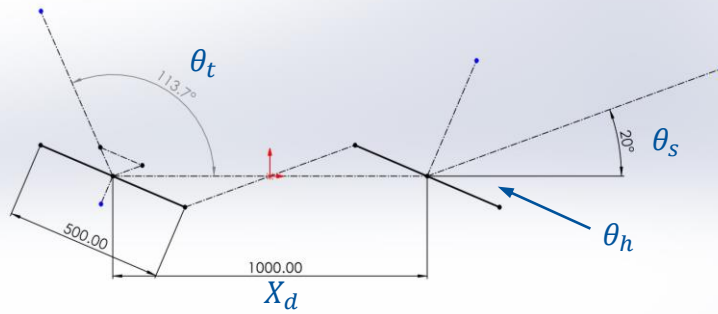


# Base Subsystem

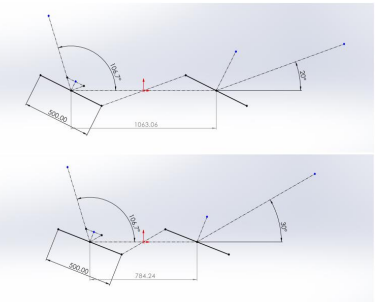
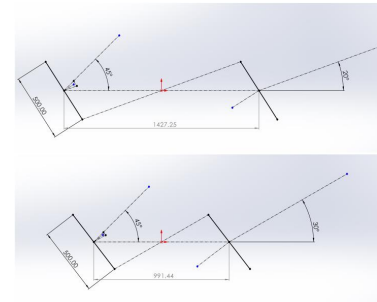
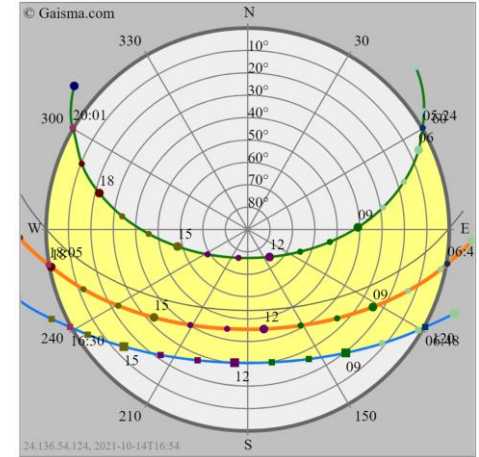
Heliostat Spacing,  $X_d$

$$\theta_h = 90 - \frac{\theta_s + \theta_t}{2}$$

$$X_d = 2 \left( \frac{s}{2} \cos(\theta_h) + \frac{\frac{s}{2} \sin(\theta_h)}{\tan(\theta_s)} \right)$$

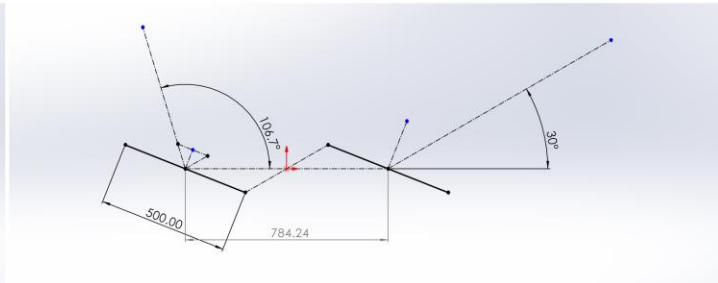
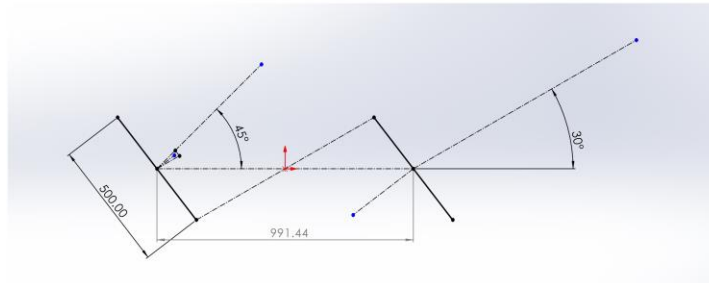
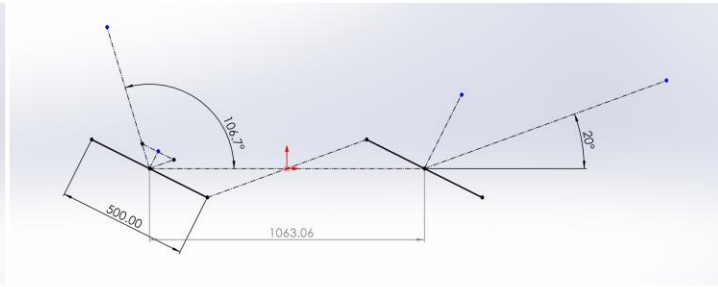
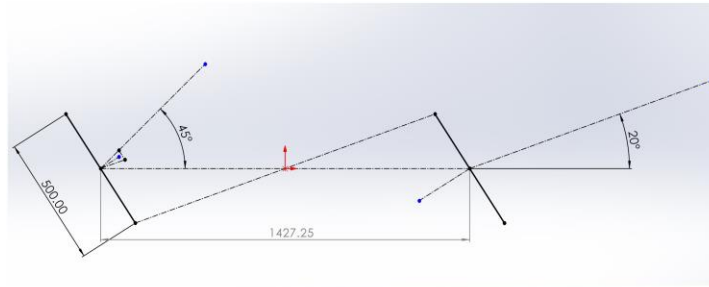


Elevation angles of the sun throughout day



# Base Subsystem

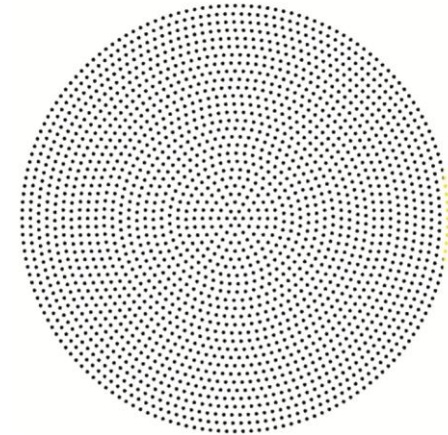
## Heliostat Spacing, $X_d$



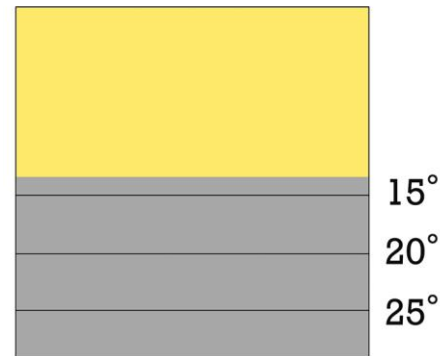
# Base Subsystem

Heliostat Spacing,  $X_d$

- 1m compromise
- No shading 30-30
- At least 30% field not shaded at all times from 20-20
- Less than half the field shaded by 25°



14 deg



# Base Subsystem

## Wind Force – Design

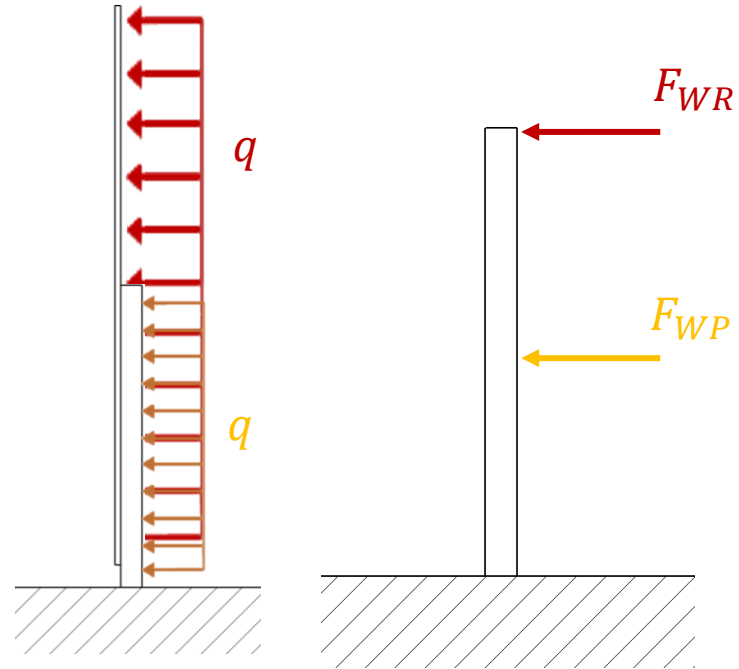
$$q = \frac{1}{2} \rho v^2 = 995.35 \text{ Pa}$$

$$F_{WR} = qA_R = 248.84 \text{ N}$$

$$F_{WP} = qA_P = qwh = 248.84w \text{ N}$$

$$M_t = (F_{WR} \times h) + \left( F_{WP} \times \frac{h}{2} \right)$$

$$I = \frac{1}{12} (w^4 - (w - 2t)^4) \quad \sigma_w = \frac{My}{I}$$

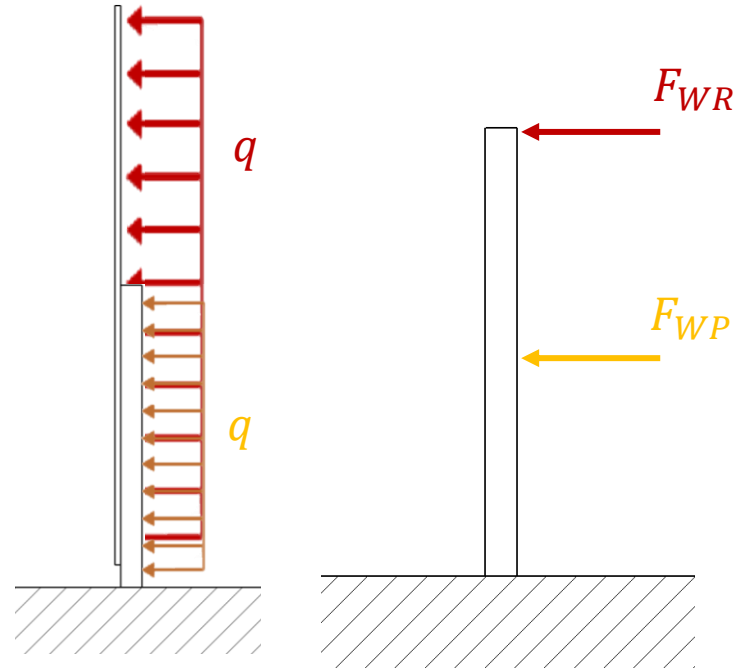


# Base Subsystem

## Wind Force – Design

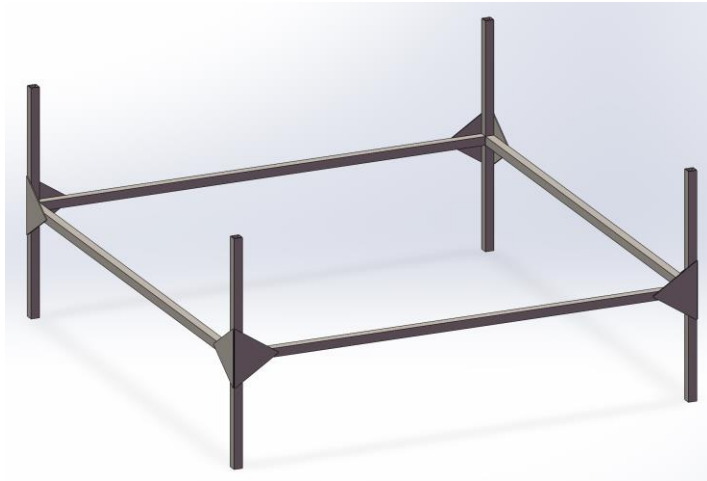
$$n = \frac{\sigma_y}{\sigma_w}$$

- With  $t = 1.27\text{mm}$  and  $n = 2$ 
  - Aluminum –  $w \geq 18.21\text{mm}$
  - Steel –  $w \geq 16.35\text{mm}$
- $\frac{3}{4}'' \times \frac{3}{4}'' \times 18\text{GA}$  square steel tube
- Cost  $\approx \$1.17$  per foot

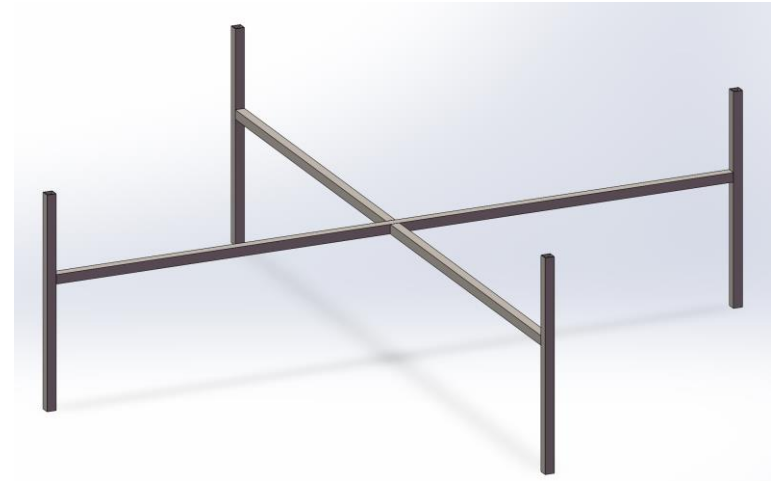


# Base Subsystem

## Design Progression



- 6 meters of bar stock
- 8 corner gussets
- Computer mounting on one side



- 4.5 meters of bar stock
- No corner gussets
- Same distancing
- Looks cool



## Base Subsystem

Gussets – Have or Have Not

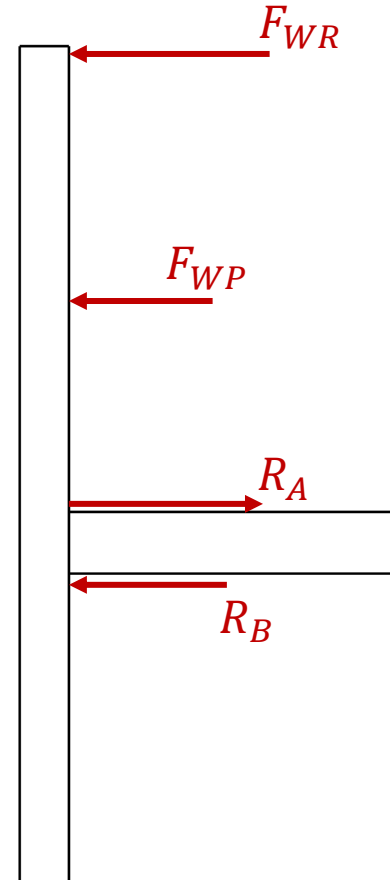
- Weld Gussets
- Rivet/Bolt Gussets
- Weld Crossbars (no gussets)

$$\Sigma M_B = 0$$

$$F_{wr}(h + w) + F_{wp}\left(\frac{1}{2}h + w\right) = R_A w$$

$$R_A = 3532 \text{ N}$$

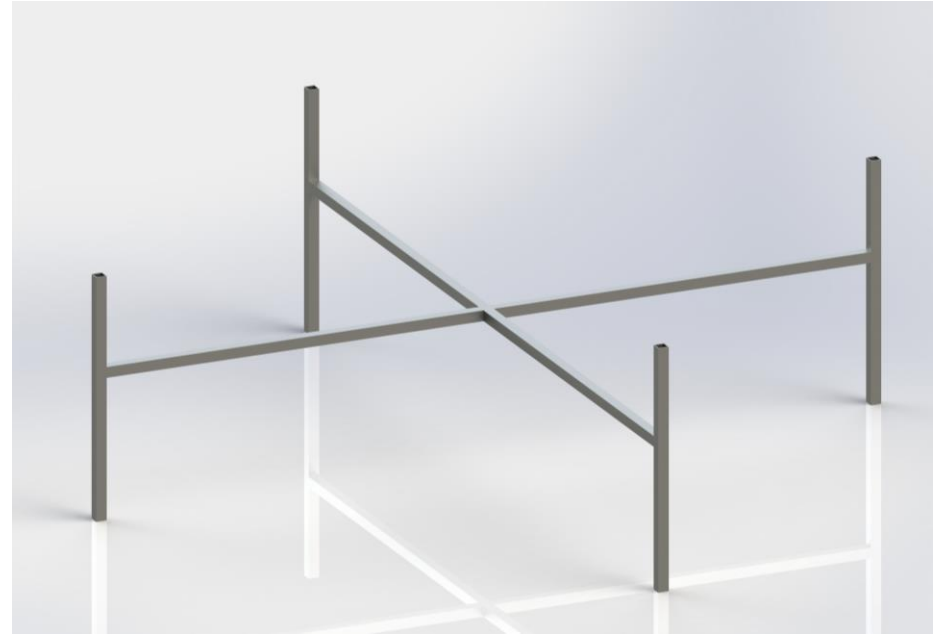
$$\sigma_A = \frac{R_A}{wt} = 146 \text{ MPa}$$



# Base Subsystem

## Final Specifications

- Bending Stress FoS,  $n = 2.8$
- Weld FoS,  $n = 2.4$
- Beam Deflection,  $\delta = 1.36 \text{ mm}$
- \$18.17 for stock



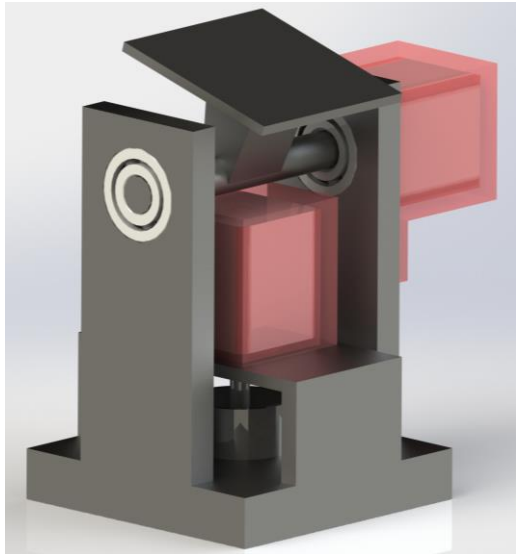
# Actuator Subsystem

## Key Features and Design Choices

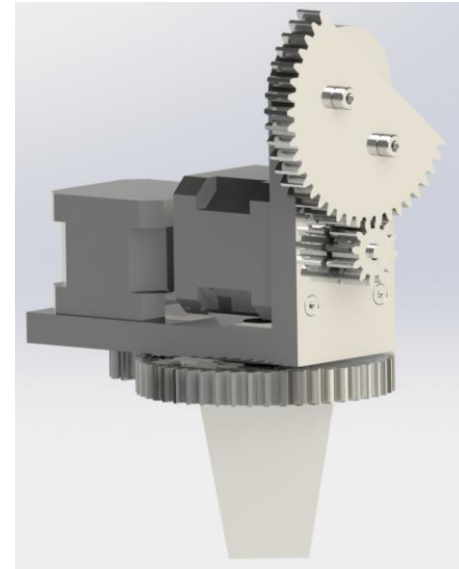
- Azimuth and Elevation rotation
- Gears increase holding torque
- Compact, Simple Design
- Plastic gears to reduce cost
- Structurally Stable



# Actuator Subsystem

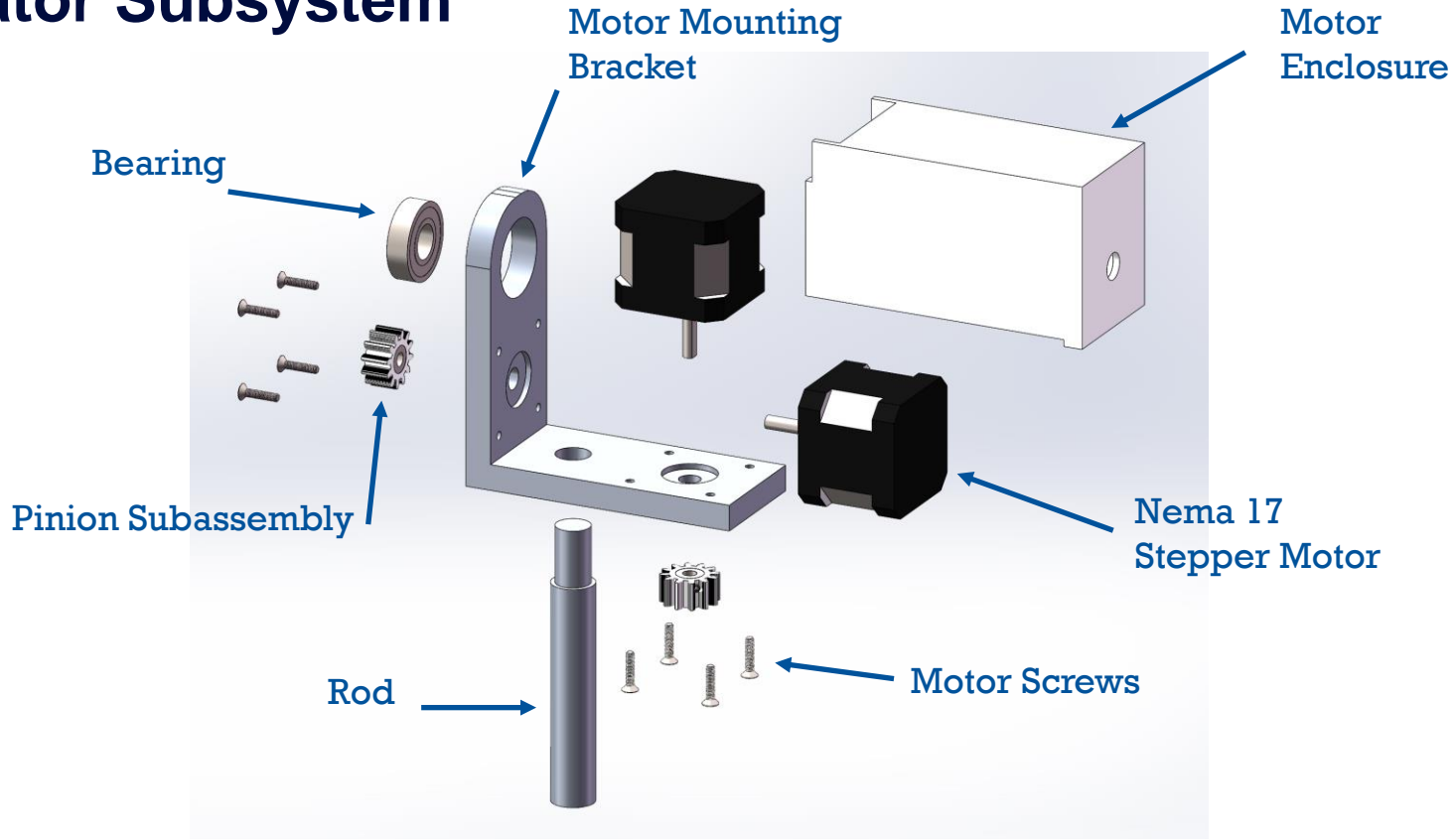


- Not strong enough .4 Nm output
- Load on motor shaft
- Costly: \$55 material and OTS



- Strong 1.6 Nm output
- No load on motor shafts
- Cheaper: \$45 material and OTS

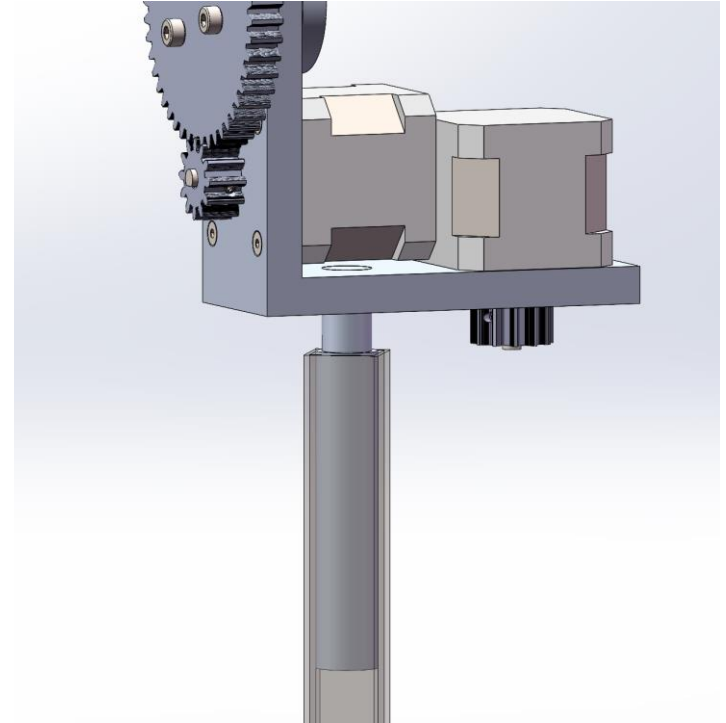
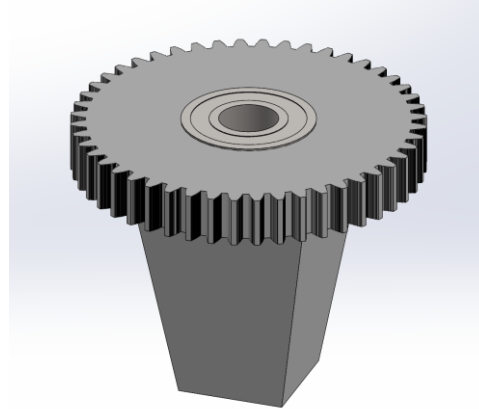
# Actuator Subsystem



# Actuator Subsystem

## Base Attachment

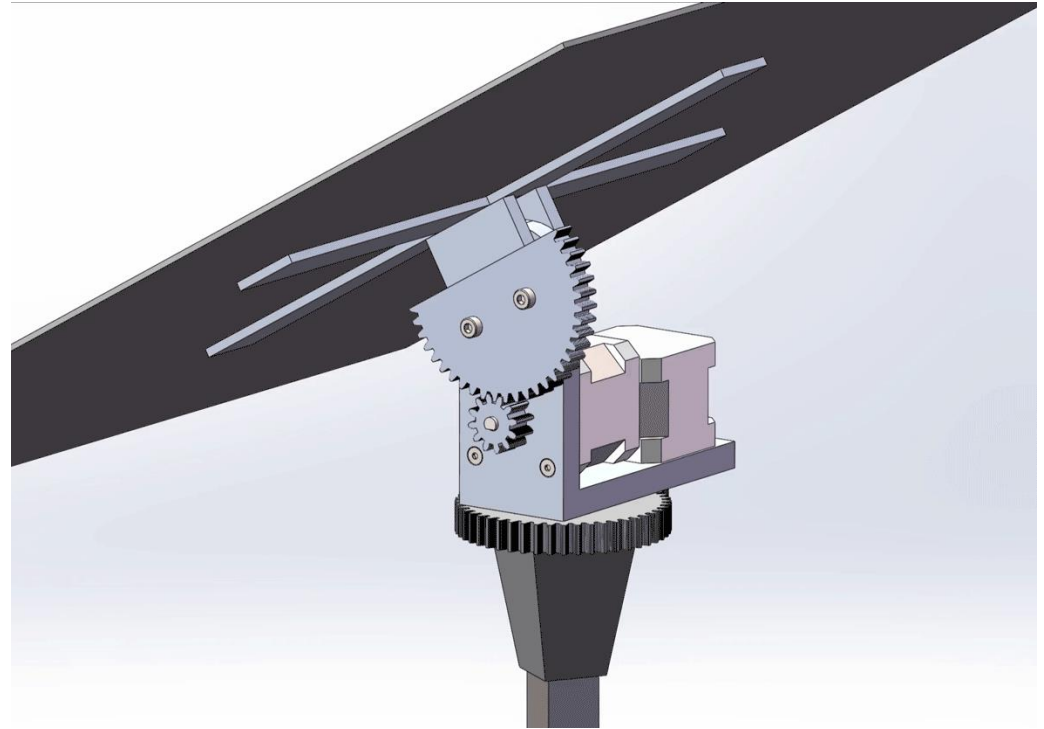
- Avoids weak bending points
- Gear doubles as adapter
- Bearing for smooth movement and stability



# Actuator Subsystem

## Functionality

- Big gear adapter remains stationary
- Azimuth motor “crawls” around the big gear
- Elevation motor drives mirror



# Actuator Subsystem

## System Analysis - Wind

$$\tau_o = GR \cdot \tau_m = 1.6 \text{ N/m}$$

$$\tau_o = (F_L + F_D) \times r$$

$$\tau_o = \frac{s}{4} (F_L \cos(\theta_h) + F_D \cos(\theta_h))$$

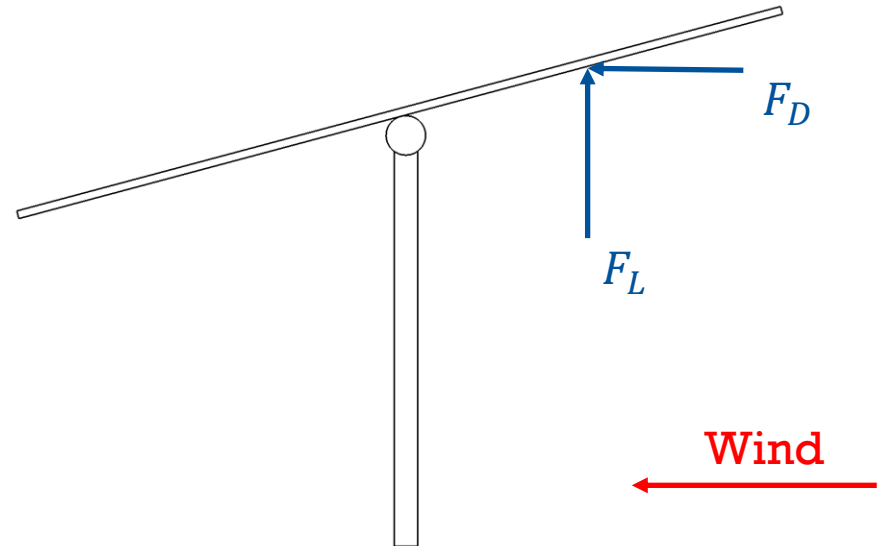
$$v \leq 8.51 \text{ m/s}, 19 \text{ mph}$$

$$F_L = \frac{C_L \rho v^2 A}{2}$$

$$C_L = 2\pi\theta_h$$

$$F_D = \frac{C_D \rho v^2 A}{2}$$

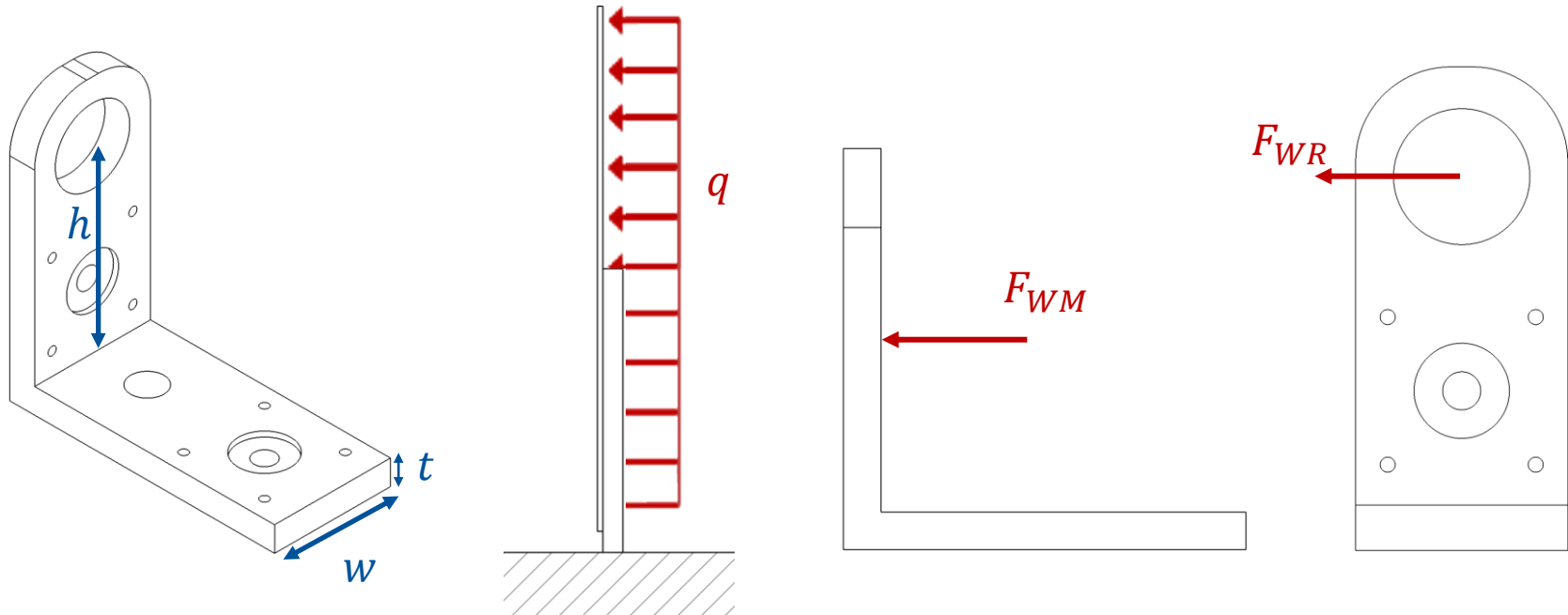
$$C_D = \frac{C_L^2}{\pi e B_{AR}}$$





# Actuator Subsystem

## Wind Force



# Actuator Subsystem

## Wind Force

$$F_{WR} = 248.84 \text{ N}$$

$$M_M = F_{WM}h = 0.271 \text{ Nm}$$

$$I_M = \frac{1}{12} (wt^3)$$

$$\sigma_M = \frac{M_M \frac{t}{2}}{I_M} = 0.403 \text{ MPa}$$

$$q = 995.35 \text{ Pa}$$

$$F_{WM} = qA_P = qwh = 3.933 \text{ N}$$

$$M_R = F_{WR}h = 1.17 \text{ Nm}$$

$$I_R = \frac{1}{12} (tw^3)$$

$$\sigma_R = \frac{M_R \frac{w}{2}}{I_R} = 0.373 \text{ MPa}$$

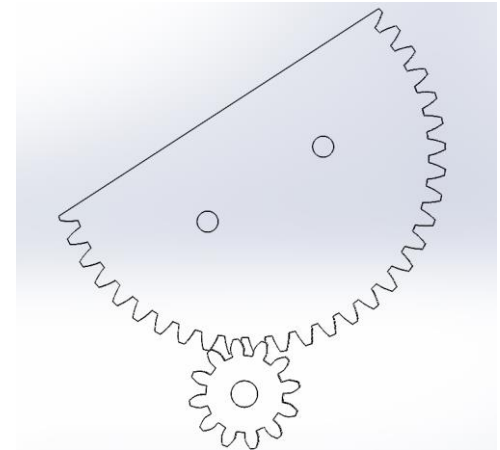
# Actuator Subsystem

## System Analysis

$$k_v = \frac{C_1 + \nu}{C_1} \quad W_t = \frac{\tau_i}{r_i} \quad r_i = r_{ip} \sin(\phi_c)$$

$$\sigma_b = k_v \frac{W_t}{lMY} = 16.4 \text{ kPa}$$

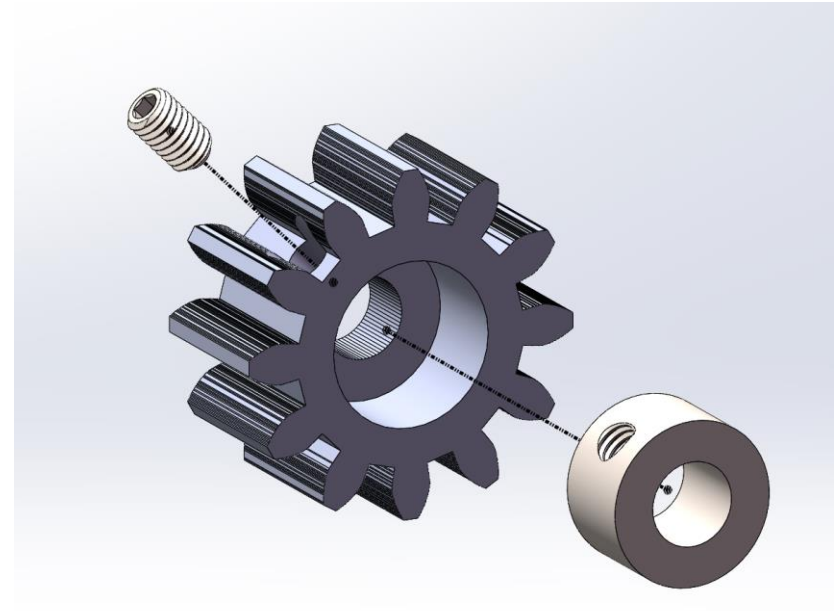
$$\sigma_c = - \left[ \frac{W_t \left( \frac{1}{r_1} + \frac{1}{r_2} \right)}{\pi l \cos(\phi_c) \left( \frac{1 - \nu_1^2}{E_1} + \frac{1 - \nu_2^2}{E_2} \right)} \right]^{\frac{1}{2}} = -40.4 \text{ MPa}$$



# Actuator Subsystem

## Pinion Gear Subassembly

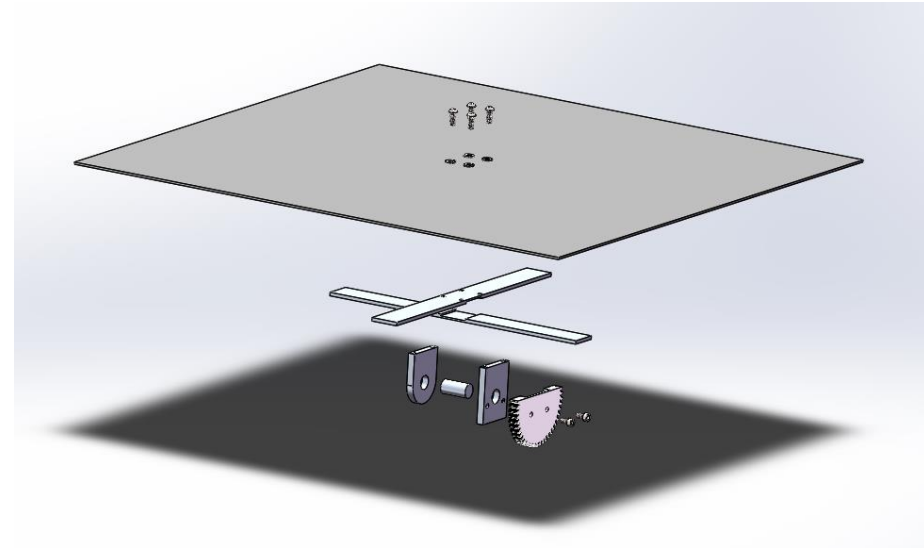
- Concerned about strength of ABS plastic gears
- Use shaft collar for attachment to motor



# Reflector Subsystem

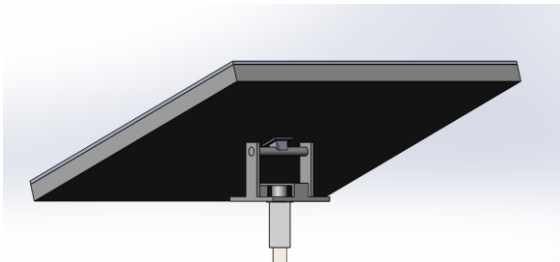
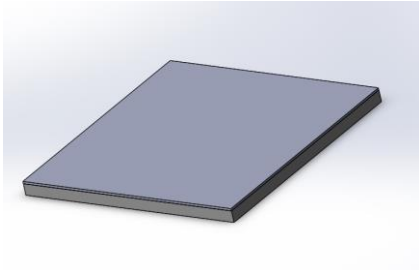
## Key Features and Design Choices

- Acrylic
- Lightweight
- Cheap
- Resistant to breaking
- Washable
- Highly reflective
- Backing support to avoid bending
- Screwed directly in

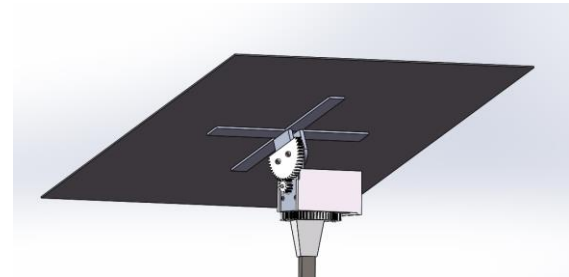
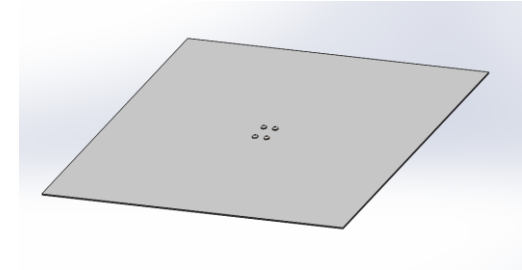


# Reflector Subsystem

## Design Progression

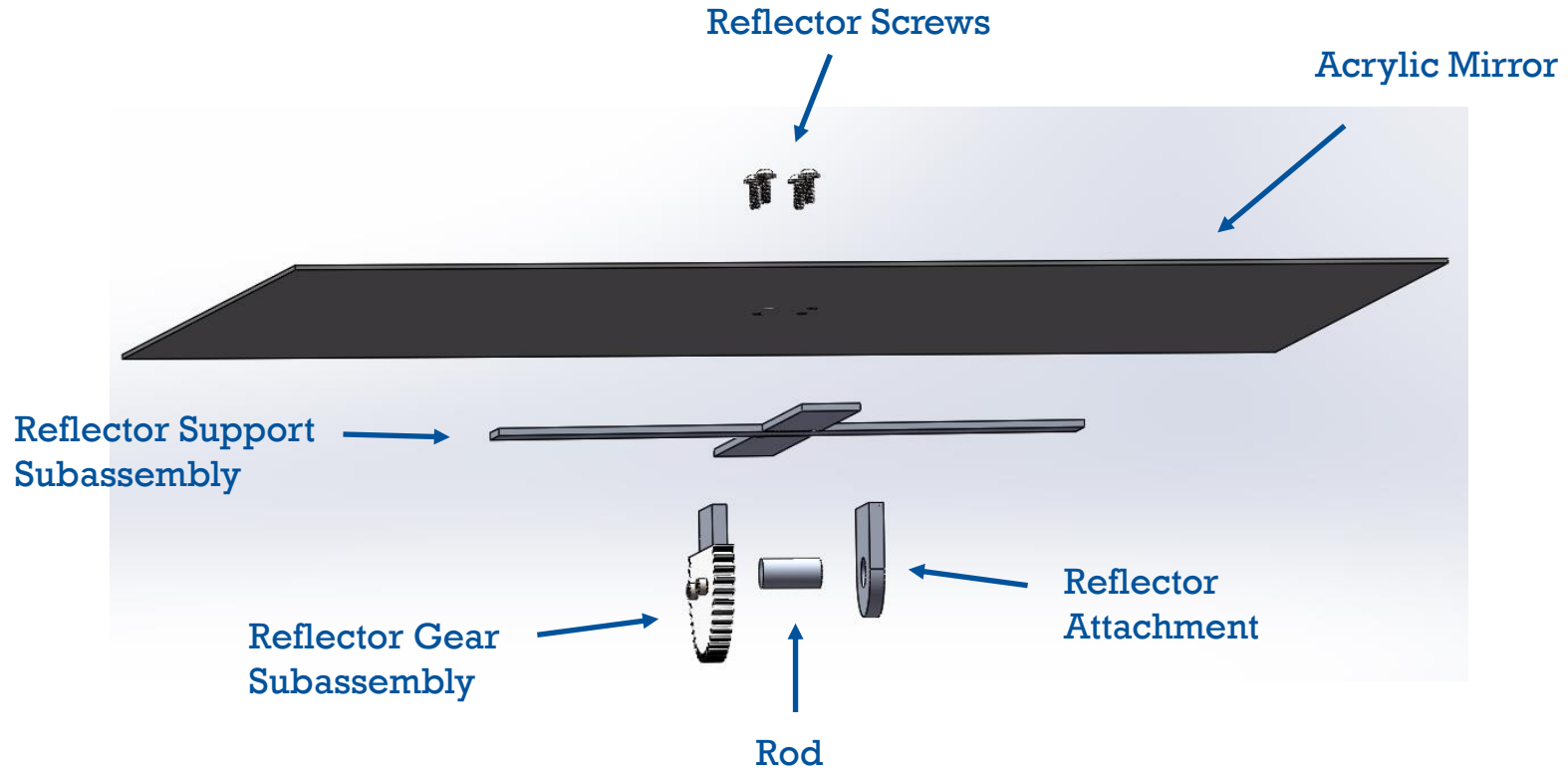


- More expensive
- Excessive support material
- Heavier



- Cheaper
- Minimalistic support design
- More lightweight

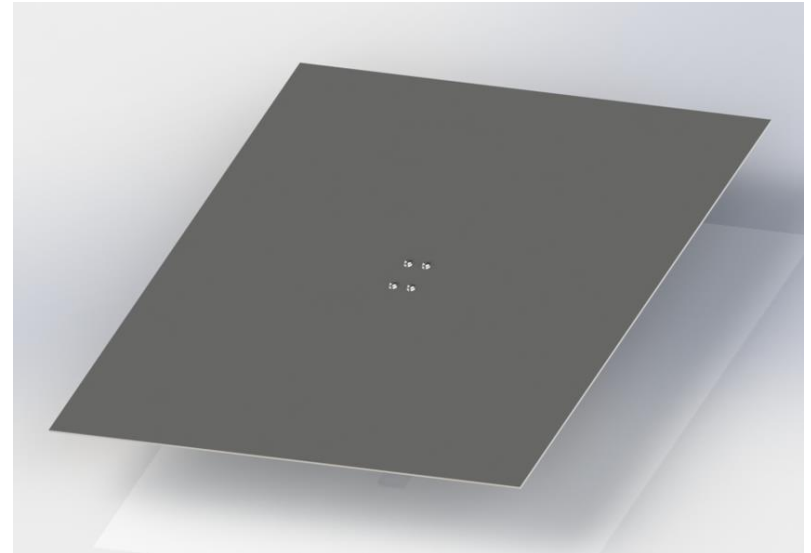
# Reflector Subsystem



# Reflector Subsystem

## Reflectivity

- Thermal Input Capability:  $P_{\text{input}} = P_{\text{solar}} A_{\text{total}} \varepsilon = 900\text{W}$ 
  - $P_{\text{solar}} = \text{Solar constant} = 1000 \text{ W/m}^2$
  - $A_t = \text{Total collection area} = 1 \text{ m}^2$
  - $\varepsilon = \text{optical efficiency} = 90\%$





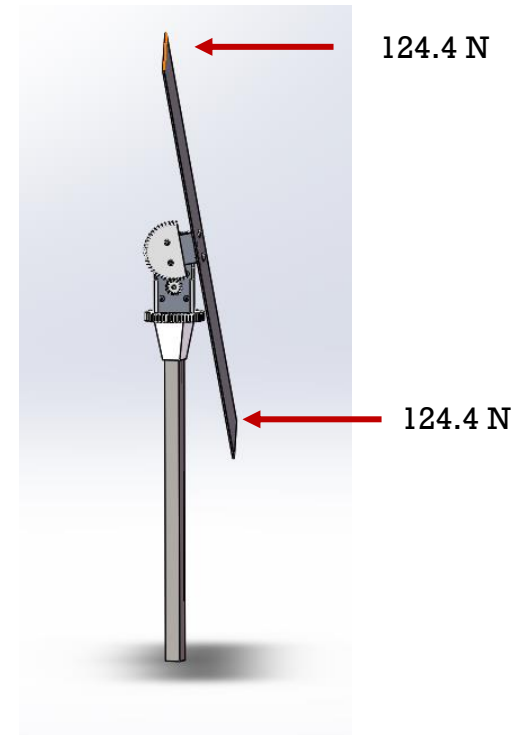
# Reflector Subsystem

## Bending Stress due to 40 m/s wind

- Wind Force:  $F = qA = 124.4 \text{ N}$ 
  - $q = \text{Dynamic pressure} = 995.35 \text{ Pa}$
  - $A = 0.125 \text{ m}^2$
- Bending Moment:  $M = (F)(x) = 62.2 \text{ N-m}$ 
  - $F = \text{Wind Force} = 124.4 \text{ N}$
  - $x = \text{Length of half of mirror} = 0.25 \text{ m}$
- Bending Stress:  $\sigma_b = \frac{(M)(y)}{I} = 233.9 \text{ MPa}$ 
  - $M = 62.2 \text{ N-m}$
  - $Y = \text{Distance to neutral axis} = 0.001 \text{ m}$
  - $I = \text{Moment of inertia} = 2.66 * 10^{-10} \text{ m}^4$

Bending Stress due to 8.5 m/s wind: 10.4 MPa

Bending Stress due to 3.8 m/s wind: 2.1 MPa



# Reflector Subsystem

Deflection due to 40 m/s wind

- Deflection:  $\delta = \frac{FL^3}{3EI} = 106 \text{ mm}$ 
  - $F = \text{Wind force} = 124.4 \text{ N}$
  - $L = \text{Length of half of mirror} = 0.25 \text{ m}$
  - $E = \text{Elastic modulus} = 68.9 \text{ GPa}$
  - $I = \text{Moment of inertia} = 2.66 * 10^{-10} \text{ m}^4$

Deflection due to 8.5 m/s wind: 1.5 mm

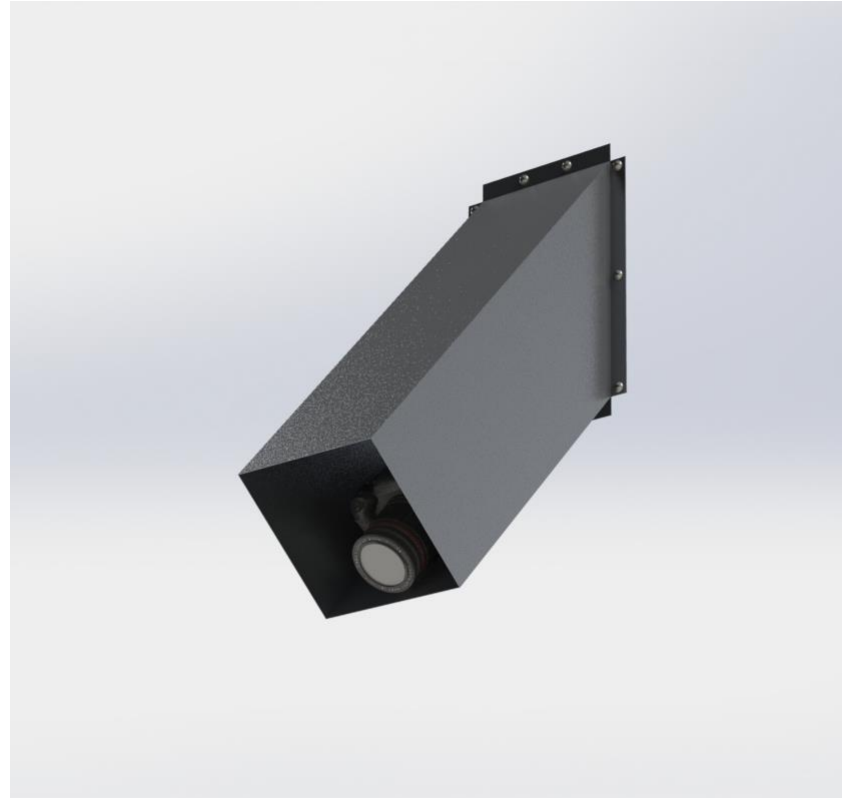
Deflection due to 3.8 m/s wind: 0.315 mm



# Tracking Subsystem

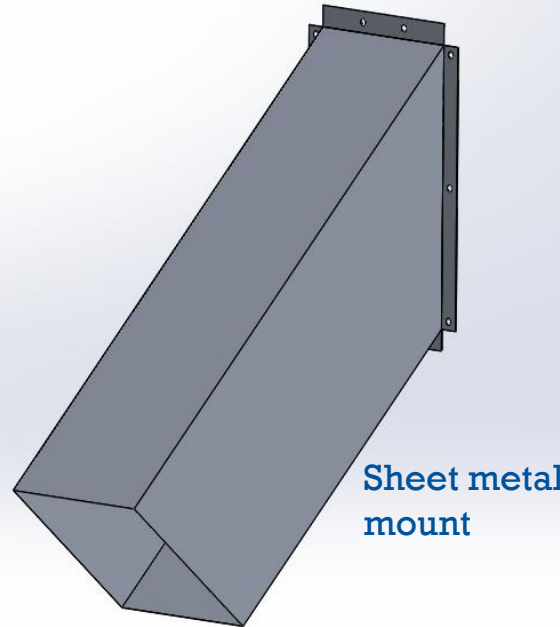
## Key Features and Design Choices

- Nikon D2X Camera
- Sheetmetal Mount for weather protection
- Improved accuracy, average 3mrad uncertainty
- Closed loop feedback control



# Tracking Subsystem

Mounting Screws



Sheet metal  
mount

Nikon D2X  
Camera



Camera  
Screw



# Tracking Subsystem

## System Analysis: Edge Detection

- Calculated angles and length ratios

$$\theta_1 = a \cos \frac{a \cdot b}{|a||b|}$$

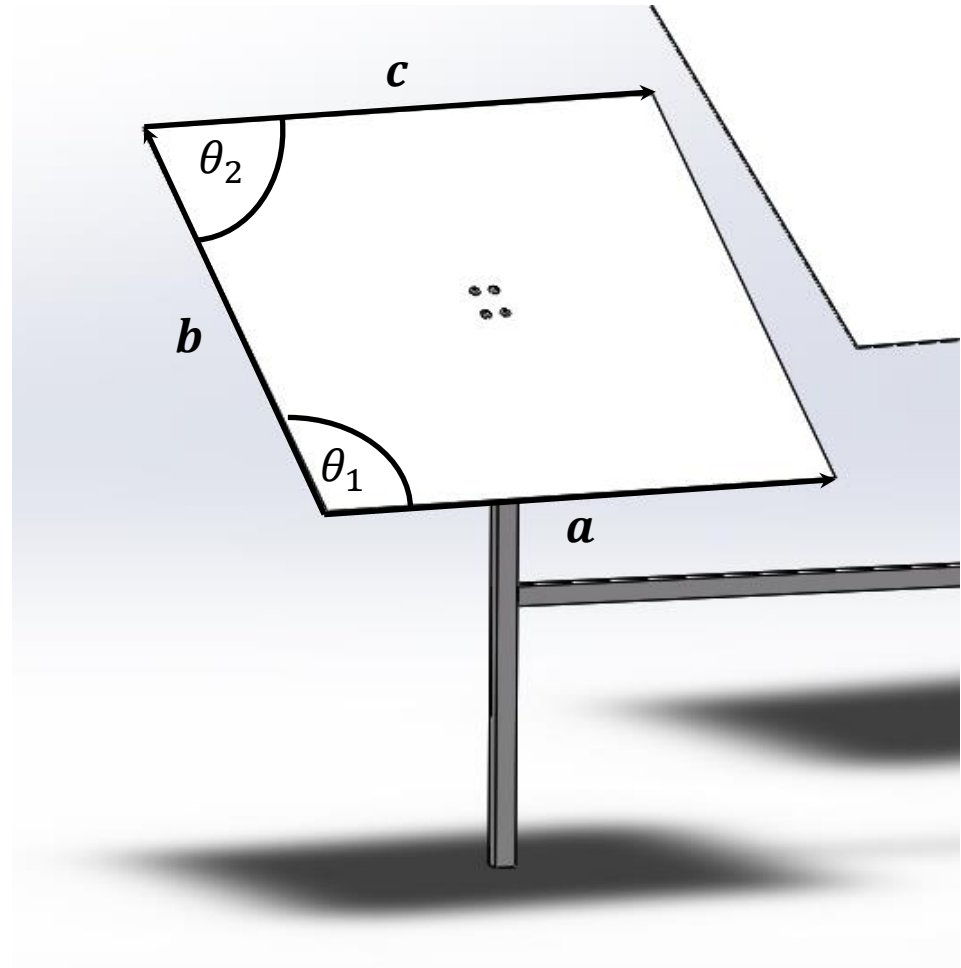
$$\theta_1 = a \cos \frac{-b \cdot c}{|b||c|}$$

$$\phi_1 = \frac{|b|}{|a|}$$

$$\phi_2 = \frac{|c|}{|a|}$$

- Global maximum difference
  - $C_k = \phi$  and  $\theta$  values
  - $\sigma_k =$  weighing factor
  - $A, \alpha =$  altitude and azimuth angles

$$N^{-1} = \sum_{k=1}^4 \frac{[C_{k,meas} - C_{k,calc}(A, \alpha)]^2}{\sigma_k}$$

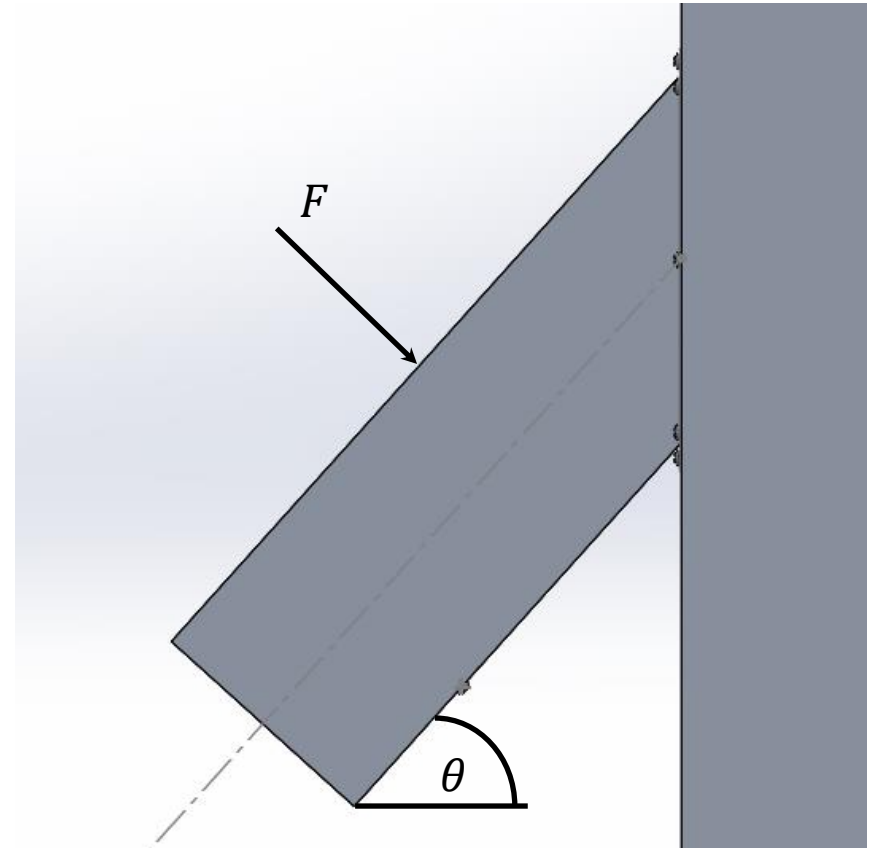


# Tracking Subsystem

## System Analysis:

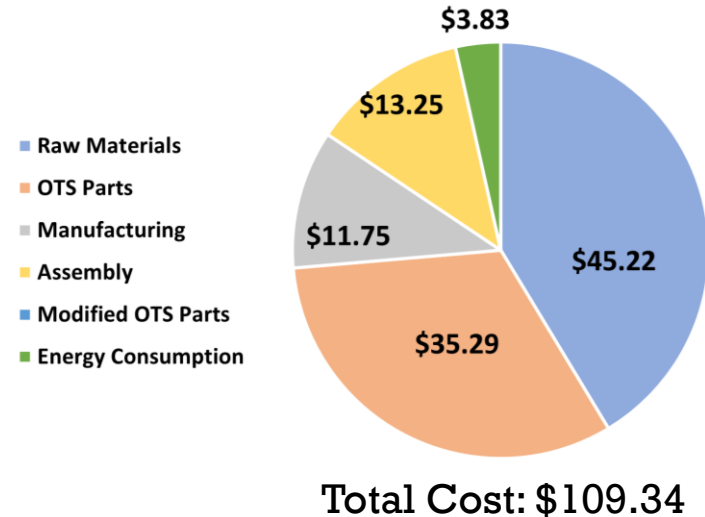
### Sheetmetal wind resistance

- Wind Force:  $F = qA = 98.01 \text{ N}$ 
  - $q$  = Dynamic pressure = 995.35 Pa
  - $A$  = top side area = .098 m<sup>2</sup>
- Bending moment:  $M = F \left( \frac{L}{2} \right) = 26.60 \text{ Nm}$ 
  - $L$  = length of top = .54 m
  - $\theta$  = 48 degrees
- Bending Stress:  $\sigma_b = \frac{(M)(y)}{I} = 0.652 \text{ MPa}$ 
  - $y$  = 0.0875 m
  - $I$  =  $3.567 \times 10^{-6} \text{ m}^4$



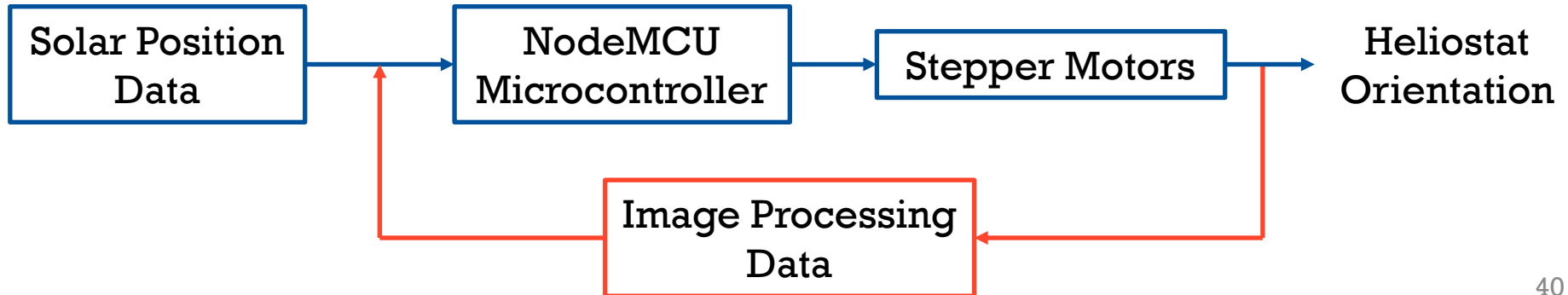
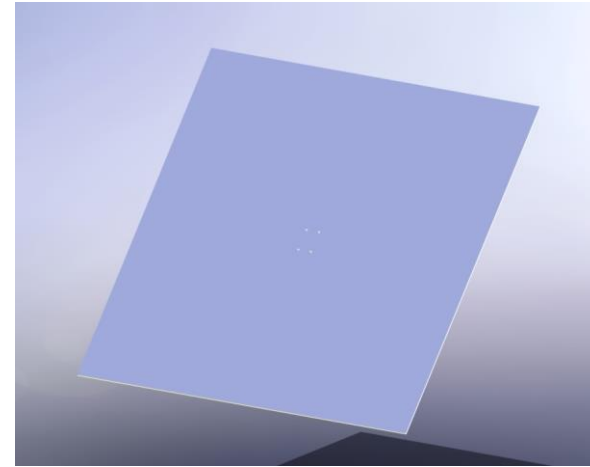
# Cost Overview

Subsystem Materials	Cost
Base	\$18.17
Actuator	\$45.24
Reflector	\$14.51
Tracking System	\$2.58
<b>Total</b>	<b>\$80.50</b>



# Design Highlights

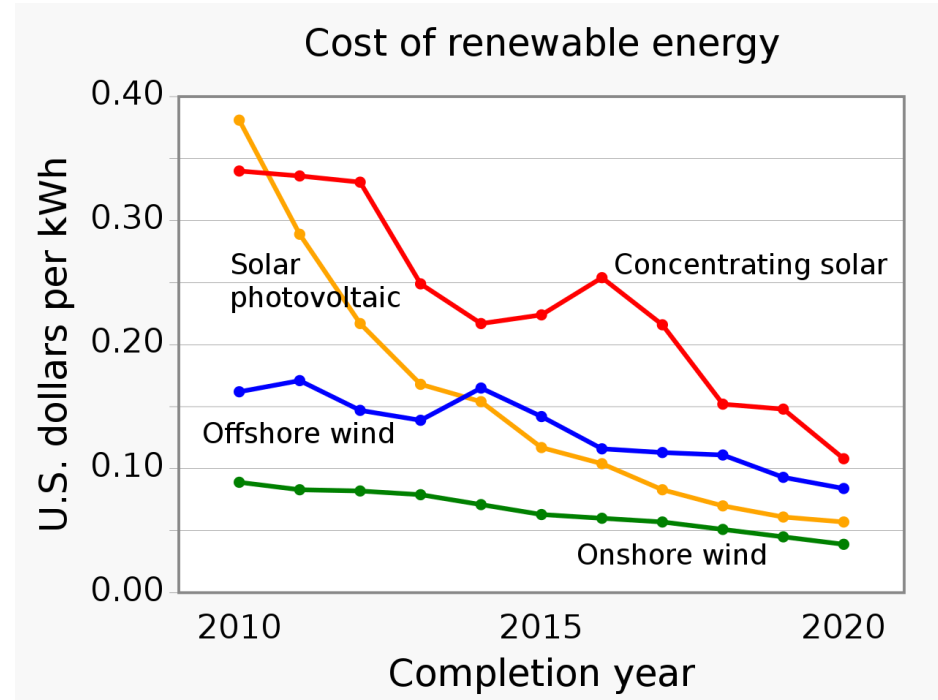
- Acrylic Mirrors
- Gear Reduction
- Tracking System





# Why Accu-Stat?

Efficiency.



Source: International Renewable Energy Agency

# Conclusion

## Key Takeaways:

- Extremely accurate design (4 mrad uncertainty)
- Optimized frame to reduce material amount
- Lightweight, low-cost acrylic mirror



## Thank You

We would like to thank our corporate sponsors Cummins, Northrop Grumman, Carrier, and Aurigo for their support on this project.

